Merging CompuCell3D and SBW/SBML

Julio M. Belmonte

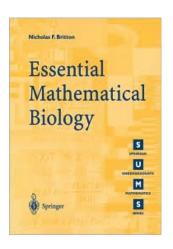
Indiana University, Bloomington

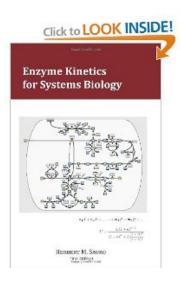
Outline

- Objectives
- Ways to add RK to CC3D
- SBML format
- Generating SBML using Jarnac
 - Simple Oscillator
- Integrating with CC3D
 - Bionet example simple oscillator
 - Adding Cell Cycle model from <u>sbml.org</u>
 - John Tyson's Cell Cycle model
 - Collier et al. Delta-Notch patterning model

More on Reaction Kinetics Modeling

Essential Mathematical Biology Nicholas Britton





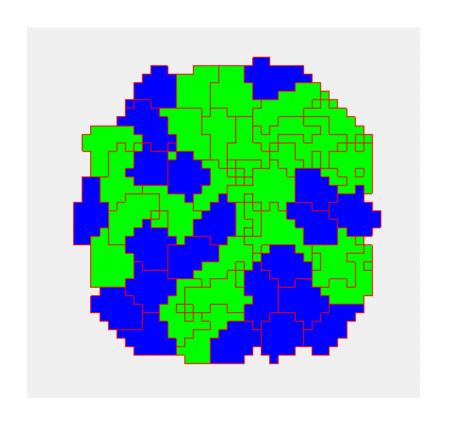
Enzyme Kinetics for Systems Biology
Herbert Sauro

www.sys-bio.org/sbwWiki/tutorials/bloomington2011

Cell-based modeling

Cellular behaviors:

- Location
- Volume
- Shape
- Movement
- Adhesion
- Mitosis
- Death
- Differentiation
- Polarization
- Etc...

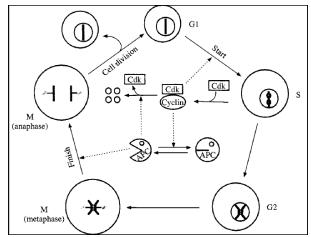


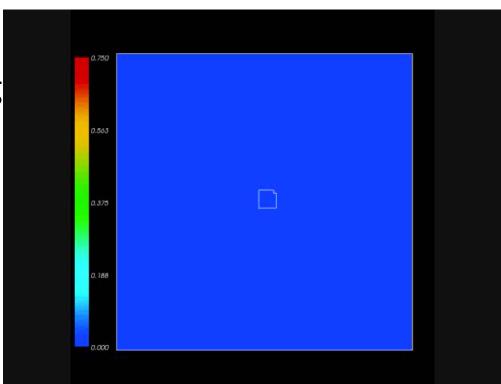
Subcellular modelling

- Biochemical Kinetics:
 - Cell-Cycle
 - Circadian rhythms
 - Cardiac rhythms
 - cAMP oscillations
 - Delta-Notch patterning
 - WNT pathway
 - FGF pathway
 - Etc...

Subcellular modelling

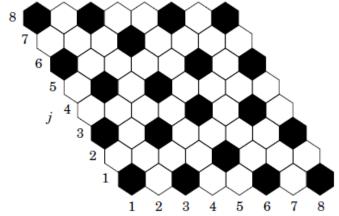
- Biochemical Kinetics:
 - Cell-Cycle
 - Circadian rhythms
 - Cardiac rhythms
 - cAMP oscillations
 - Delta-Notch patterning
 - WNT pathway
 - FGF pathway
 - Etc...

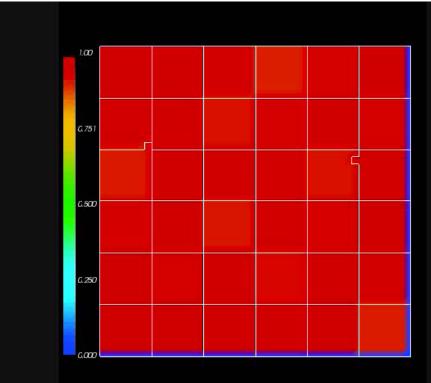




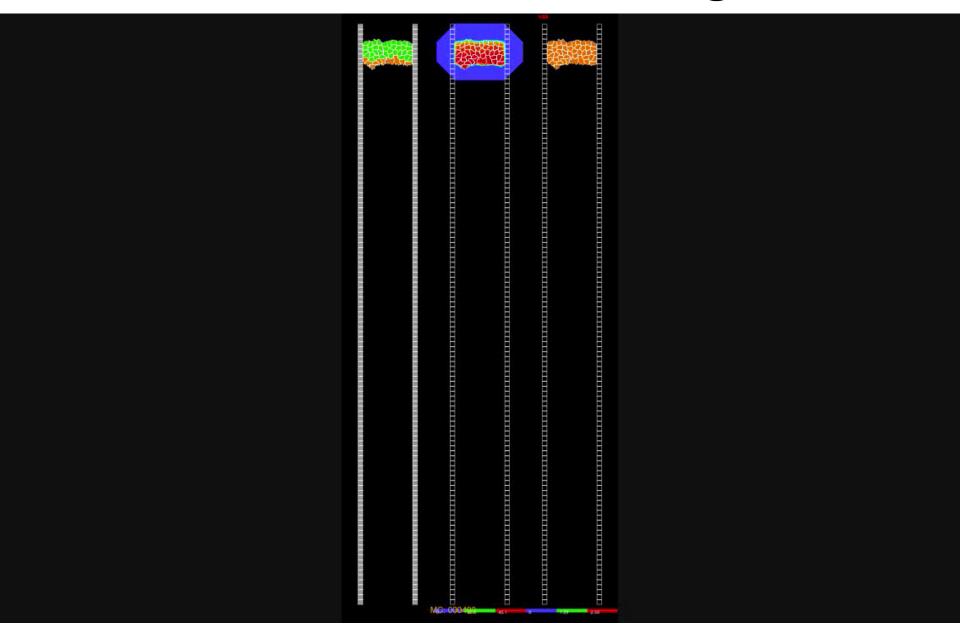
Subcellular modelling

- Biochemical Kinetics:
 - Cell-Cycle
 - Circadian rhythms
 - Cardiac rhythms
 - cAMP oscillations
 - Delta-Notch patterning
 - WNT pathway
 - FGF pathway
 - Etc...





Multiscale model - Somitogenesis



How to add this into CompuCell?

- 1) Just another Python class!
 - Too slow

How to add this into CompuCell?

- 1) Just another Python class!
 - Too slow

- 2) C++ file to be wrapped into Python
 - Too complicated

How to add this into CompuCell?

- 1) Just another Python class!
 - Too slow

- 2) C++ file to be wrapped into Python
 - Too complicated
- 3) Import SBML

SBML – Systems Biology Markup Language

Not a software!

 Machine-readable format for representing subcellular models

Standard for storage and exchange of models

Implementation agnostic

How does it work?

Developer software (SBW/Jarnac)



SBML



Simulation software (CompuCell3D)

$$S_1 \xrightarrow{k} 2 \cdot S_2$$

• Initial conditions:

$$S_1 = 5 \text{ nM}$$

$$S_2 = 0$$
 nM

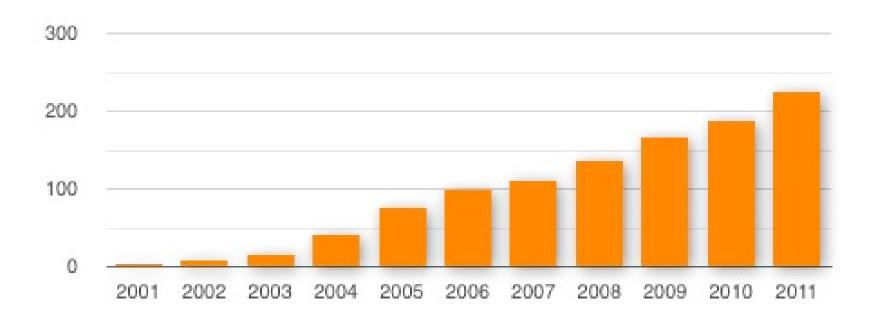
• Parameters:

$$k = 0.1 \text{ min}^{-1}$$

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns = "http://www.sbml.org/sbml/level2" level = "2" version = "1">
 <model id = "cell">
  <listOfCompartments>
    <compartment id = "compartment" size = "1"/>
  </listOfCompartments>
  listOfSpecies>
     <species id = "S1" boundaryCondition = "false" initialConcentration = "5.0" compartment = "compartment"/>
     <species id = "S2" boundaryCondition = "false" initialConcentration = "0.0" compartment = "compartment"/>
  </listOfSpecies>
  <listOfParameters>
    </listOfParameters>
  listOfReactions>
    <reaction id = " J1" reversible = "false">
     listOfReactants>
      <speciesReference species = "S1" stoichiometry = "1"/>
     </listOfReactants>
     IistOfProducts>
      <speciesReference species = "S2" stoichiometry = "2"/>
     <kineticLaw>
      <math xmlns = "http://www.w3.org/1998/Math/MathML">
        <apply>
         <times/>
          <ci>
            k1
          </ci>
          <ci>
            S1
         </ci>
        </apply>
      </kineticLaw>
    </reaction>
  </listOfReactions>
 </model>
```

</sbml>

 Total number of known SBML-compatible software packages each year :



How to write SBML?

Bio-Spice

• Large collection of tools, integrated via a "Dashboard." Free download (BSD), various platforms.

Teranode

• Suite of tools for model management, design, and simulation. (Linux/Mac/Windows) Commercial (30-day trial available).

• SBW

- Systems Biology Workbench.
- Check http://sbml.org/SBML Software Guide

SBW/Jarnac

- SBW Systems Biology Workbench:
 - Open-source software framework for systems biology

- Jarnac:
 - Software for writing and simulating reaction kinetics
 - Easy to use
 - Translate to SBML (C++, Matlab, Mathematica, etc..)

Download at: http://www.sys-bio.org/

Integration with CC3D

 Reaction kinetic models can be easily added in CC3D when in SBML format.

- Once loaded, the model is converted into a set of ODEs and is solved by the BionetSolver library inside CC3D.
- The commands used to load and manipulate the models inside CC3D are summarized on the "Quick Reference Guide" for Python in CC3D.

Integration with CC3D

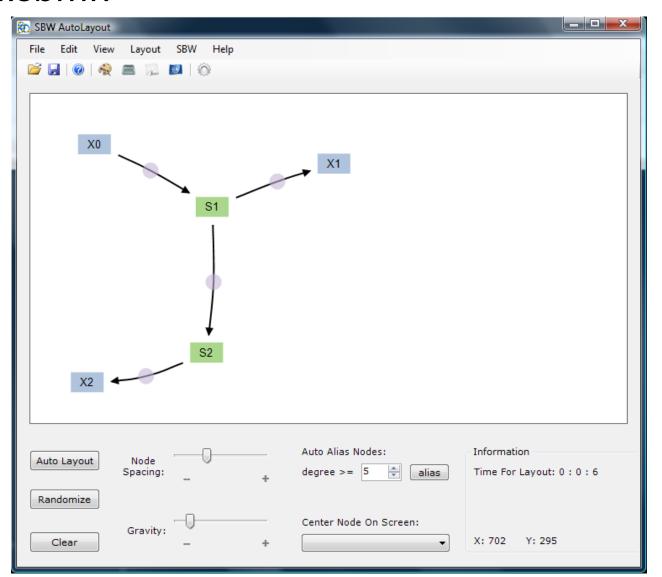
```
import bionetAPI # Import bionetAPI functions
class <someClass>(SteppableBasePy):
 def init (self, simulator, frequency=1):
   SteppableBasePy. init (self, simulator, frequency)
   bionetAPI.initializeBionetworkManager(self.simulator) # Initialize bionet inside class
 def start(self):
   # Load a specific subcellular SBML submodel
   ModelName = <sbmlModelName>
                                 # Name of the model
   ModelPath = <sbmlModelPath> # Path where the model is stored
                            # Nickname of the model
   ModelKey = <modelKey>
   IntegrationStep = <timeStep> # Time step of integration
   bionetAPI.loadSBMLModel( ModelName, ModelPath, ModelKey, IntegrationStep )
   # Add SBML submodel to a group of cells or a single cell
   bionetAPI.addSBMLModelToTemplateLibrary(<sbmlModelName>, {<cellType> or <cellId>})
   # Modify the parameter value or molecular concentration of a cell (or group of cells)
   bionetAPI.setBionetworkValue(<molecule/parameter>, <value>, {<cellType> or <cellId>})
   # Initialize model
   bionetAPI.initializeBionetworks()
 def step(self, mcs):
   # Iterate the model (run it for the time step specified on the load command)
   bionetAPI.timestepBionetworks()
   # Get the parameter value or molecular concentration from a cell (or group of cells)
    <var>=bionetAPI.getBionetworkValue({<parameter> or <molecule>}, {<cellType> or <cellId>})
   # Modify the parameter value or molecular concentration of a cell (or group of cells)
   bionetAPI.setBionetworkValue(<molecule/parameter>, <value>, {<cellType> or <cellId>})
```

Integration with CC3D

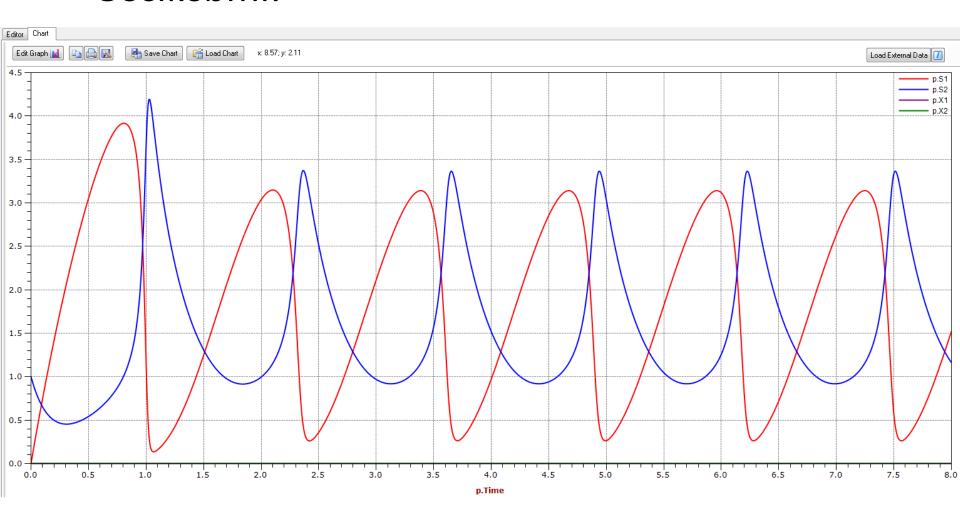
```
1 import bionetAPI # Import bionetAPI functions
   class <someClass>(SteppableBasePy):
     def init (self, simulator, frequency=1):
        SteppableBasePy. init (self, simulator, frequency)
2 --> bionetAPI.initializeBionetworkManager(self.simulator) # Initialize bionet inside class
     def start(self):
        # Load a specific subcellular SBML submodel
ModelName = <sbmlModelName> # Name of the model
ModelPath = <sbmlModelPath> # Path where the model is stored
ModelKey = <modelKey> # Nickname of the model
IntegrationStep = <timeStep> # Time step of integration
bionetAPI.loadSBMLModel( ModelName, ModelPath, ModelKey, IntegrationStep )
        # Add SBML submodel to a group of cells or a single cell
△ → bionetAPI.addSBMLModelToTemplateLibrary(<sbmlModelName>, {<cellType> or <cellId>})
        # Modify the parameter value or molecular concentration of a cell (or group of cells)
        bionetAPI.setBionetworkValue(<molecule/parameter>, <value>, {<cellType> or <cellId>})
        # Initialize model
5 ---> bionetAPI.initializeBionetworks()
     def step(self, mcs):
        # Iterate the model (run it for the time step specified on the load command)
        bionetAPI.timestepBionetworks()
        # Get the parameter value or molecular concentration from a cell (or group of cells)
        <var>=bionetAPI.getBionetworkValue({<parameter> or <molecule>}, {<cellType> or <cellId>})
        # Modify the parameter value or molecular concentration of a cell (or group of cells)
        bionetAPI.setBionetworkValue(<molecule/parameter>, <value>, {<cellType> or <cellId>})
```

- MODEL:
 - 2 cell types:
 - Condensing
 - NonCondensing
 - Condensing cells have stable volume
 - NonCondensing cells' volume oscillate
 - Volume oscillation is driven by a subcellular model:
 - Oscli.sbml

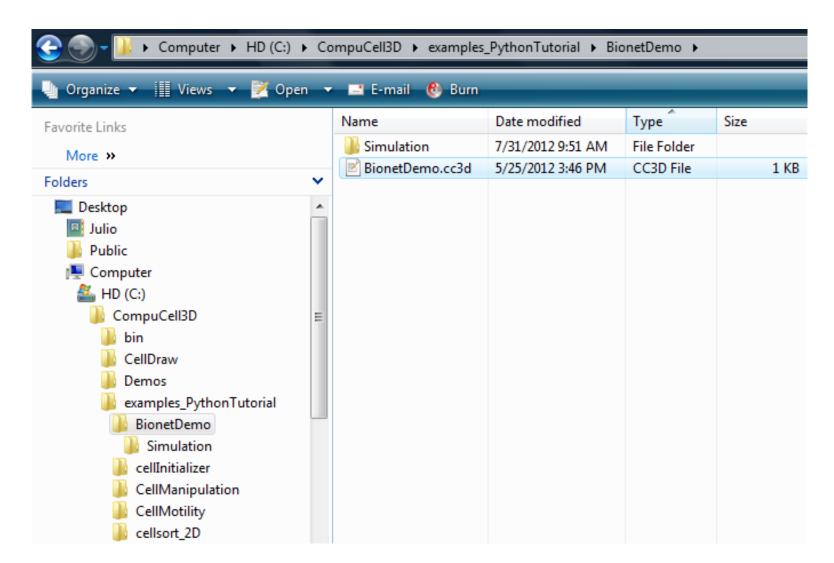
• Oscli.sbml:



• Oscli.sbml:



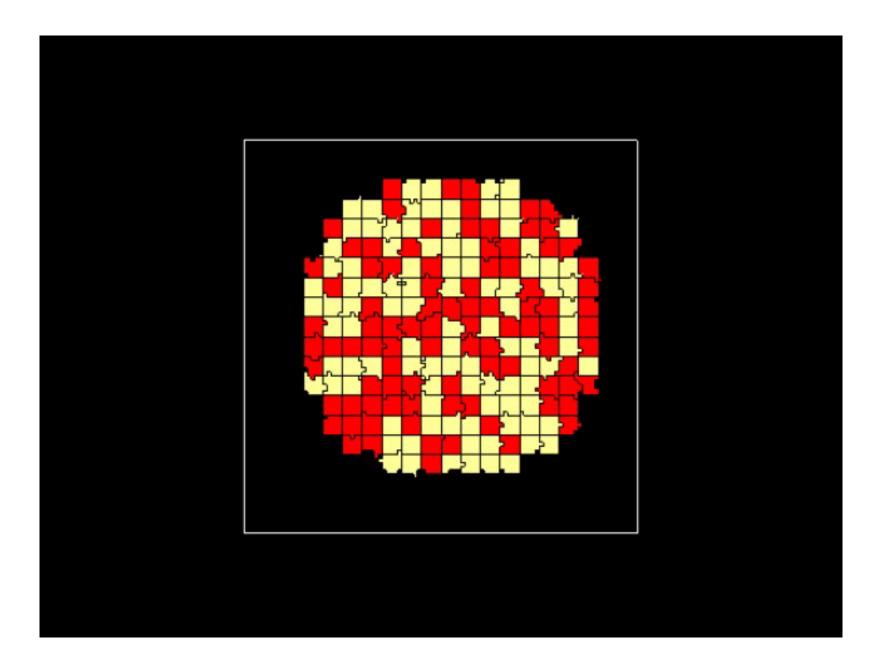
On Twedit++, open the Project File BionetDemo:



```
import bionetAPI
 7
   Eclass BionetDemoSteppable (SteppableBasePy):
10
   def init (self, simulator, frequency=10):
          SteppableBasePy. init (self, simulator, frequency)
12
            bionetAPI.initializeBionetworkManager(self.simulator)
   □ · · · def · start (self):
14
           *# iterating over all cells in simulation .....
15
           for cell in self.cellList:
            # you can access/manipulate cell properties here
17
           cell.targetVolume=25
18
19
           cell.lambdaVolume=2.0
20
21
           #bionet section
22
           · modelName = "OSCLI"
23
            modelNickname = "OSC" # this is usually shorter version version of model name
24
25
           fileDir=os.path.dirname (os.path.abspath( file ))
26
27
           modelPath=os.path.join(fileDir, "oscli.sbml")
28
           print "Path=", modelPath
29
30
           integrationStep = 0.02
31
           bionetAPI.loadSBMLModel(modelName, modelPath, modelNickname, integrationStep)
32
33
           bionetAPI.addSBMLModelToTemplateLibrary("OSCLI", "NonCondensing")
34
35
           bionetAPI.initializeBionetworks()
36
37
          # iterating over all cells in simulation .....
38
     for cell in self.cellList:
        if cell.type==self.NONCONDENSING:
40
        bionetAPI.setBionetworkValue("OSC S1",0,cell.id)
41
                   bionetAPI.setBionetworkValue("OSC S2",1,cell.id)
42
43
```

This is how we read concentration values:

```
47 | def step(self,mcs): d
```



Exercises

- 1
 - Change volume oscillation amplitude
 - Make Condensing cells oscillate
 - Make Condensing cells oscillate at opposite phase

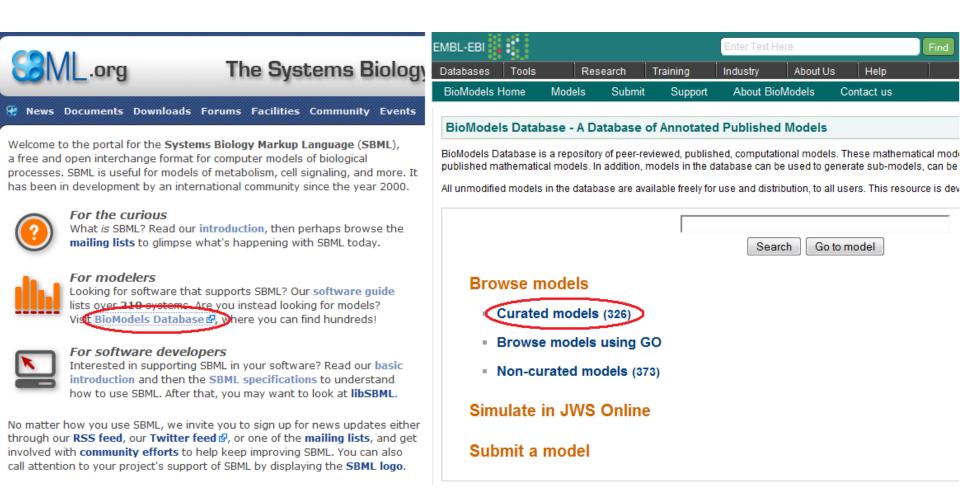
Exercises

- 1
 - Change volume oscillation amplitude
 - Make Condensing cells oscillate
 - Make Condensing cells oscillate at opposite phase
- 2
 - Replace SBML model with the one from
 Tuesday: Boris Kholodenko, <u>Eur J Biochem.</u> 2000 Mar;267(6):1583-8

- In our second example we will use a published model for the cell cycle.
- The website <u>www.sbml.org</u> contains a repository of published models in SBML format.
- If you wish to submit your own SBML to the repository, follow the instructions at: www.ebi.ac.uk/biomodels-main/submit

Second Example - Cell Cycle Model

 On www.sbml.org, click on the link "BioModels Database" and then on "Curated models":



 From the model list select the third one by clicking on the link under the column "BioModels ID"

BioModels Home Models Submit Support About BioModels Contact us Browse - Curated models

- The following fields are used to describe a model:
 - BioModels ID _ A unique string of characters associated with the model, which will never be re-used even if the model is deleted from the BioModels Database.
 - Name

 The name of the model, as written in the model itself by its creator(s).
 - Publication ID _ The unique identifier of the reference publication describing the model, specified either as a PubMed identifier (linked to the EBI Medline database), or as a DOI (linked to the original must have one publication identifier, and the same identifier can be shared amongst several models if they have been described in the same publication.
 - Last Modified

 The date when the model was last modified.

To view a model, simply click on the correspondant BioModels ID provided within the leftmost column of the row corresponding to the model.

♠ 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33

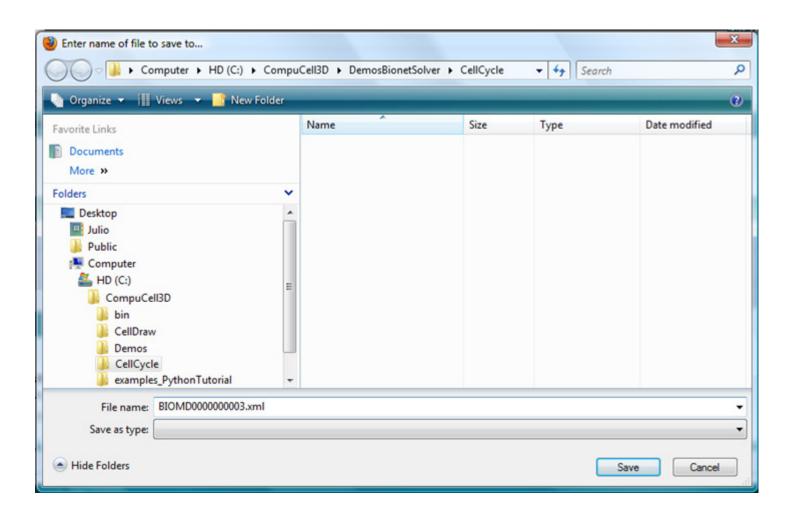
♦ □

<u>BioModels ID</u> ▽	<u>Name</u>	Publication ID
BIOMD00000001	Edelstein1996_EPSP_AChEvent	<u>8983160</u>
BIOMD000000002	Edelstein1996_EPSP_AChSpecies	<u>8983160</u>
BIOMD000000003	Goldbeter1991_MinMitOscil	<u>1833774</u>
BIOMD000000004	Goldbeter1991_MinMitOscil_ExplInact	<u>1833774</u>
BIOMD00000005	Tyson1991_CellCycle_6var	<u>1831270</u>
BIOMD000000006	Tyson1991_CellCycle_2var	<u>1831270</u>
BIOMD000000007	Novak1997_CellCycle	<u>9256450</u>
BIOMD000000008	Gardner1998_CellCycle_Goldbeter	<u>9826676</u>
BIOMD000000009	Huang1996_MAPK_ultrasens	<u>8816754</u>
BIOMD000000010	Kholodenko2000_MAPK_feedback	<u>10712587</u>

 To download the model click on "Download SBML" and select "SBML L2 V4 (curated)"

BioModels Home	Models	Submit	Support	About BioModels	Contact us		
BIOMD00000000	03 - Goldb	beter1991_M	inMitOsc	il			
$\overline{}$						٦.	
Download SBML		Other formats	(auto-gene	erated) Actions		Submit Model Comment/	Bug
SBML L2 V I (auto-ge SBML L2 V2 (auto-ge	_	Overview		Math	Physical entities	Parameters	Curation
SBML L2 V2 (auto-ge							Reference Publication
SBML L2 V4 (curated							Reference Publication
					1 Oct;88(20):9107-11.	volving cyclin and cdc2 kinase.	
Publication ID: 1833	<u>3774</u>		Goldbe		Tare militare oscillator in	volving cyclin and cdc2 kindsc.	
			Faculté	des Sciences, Unive	sité Libre de Bruxelles,	Belgium. [more]	
							Model
Original Model: <u>BIOMD000000003.xml.origin</u>		set#1	bqbiol:occursIn <u>Taxo</u>				
Submitter: <u>Nicolas Le Novère</u>				bqbiol:isVersionOf			
Submission ID: MODEL6614271263		set #2	habiol:isHomologTo	Gene Ontology mitotic of Reactome REACT 152			
Submission Date: 13 Sep 2005 12:24:56 UTC				bqbioi.isHolliolog10	REACT 132	4	
Last Modification D	ate: 17 Mar 2	2010 00:25:38 U	тс				
Creation Date: 06 F	eb 2005 23:3	39:40 UTC					
Encoders: Bruce Sh	hapiro						
Vijayalak	kshmi Chellia	<u>ah</u>					
							Notes
This a model from the		o mitotic oscilla	tor involvin	g cyclin and cdc2 kir	1300		
Goldbeter A Proc. Na					uso.		
Abstract:				and all builtings of		:- bd #	
A minimal model for	tne mitotic o	scillator is prese	entea. The r	noael, built on recent	experimental advances,	is based on the cascade of po	est-translational modification t

 Save the file BIOMD0000000003.xml anywhere in your computer, later we will transfer it to the appropriate directory.



This model is composed of 3 ODEs that forms an oscillating system:

$$\frac{dC}{dt} = v_{i} - v_{d}X \frac{C}{K_{d} + C} - k_{d}C,$$

$$\frac{dM}{dt} = V_{1} \frac{(1 - M)}{K_{1} + (1 - M)} - V_{2} \frac{M}{K_{2} + M},$$

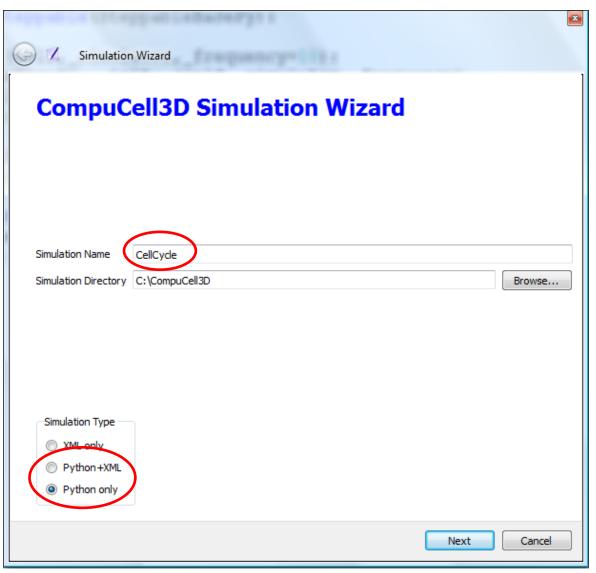
$$\frac{dX}{dt} = V_{3} \frac{(1 - X)}{K_{3} + (1 - X)} - V_{4} \frac{X}{K_{4} + X}$$

$$V_{1} = \frac{C}{K_{c} + C} V_{M1}, V_{3} = MV_{M3}.$$

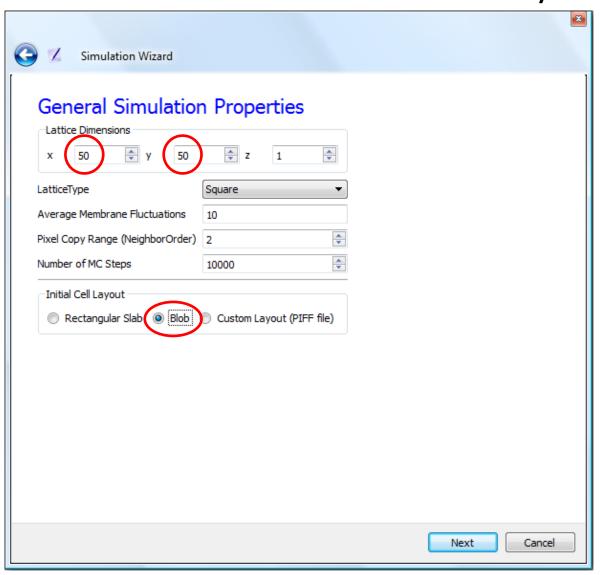
$$0.8 \frac{(N)}{(N)} = 0.8 \frac{(N)}{$$

- C : cyclin concentration
- M: fraction of active cdc2 kinase
- X : fraction of active cyclin protease

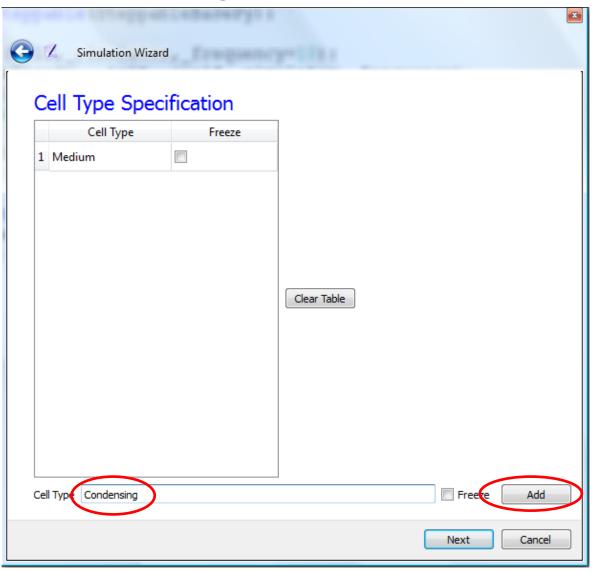
Using Tweddit++ Wizard, create a new simulation:



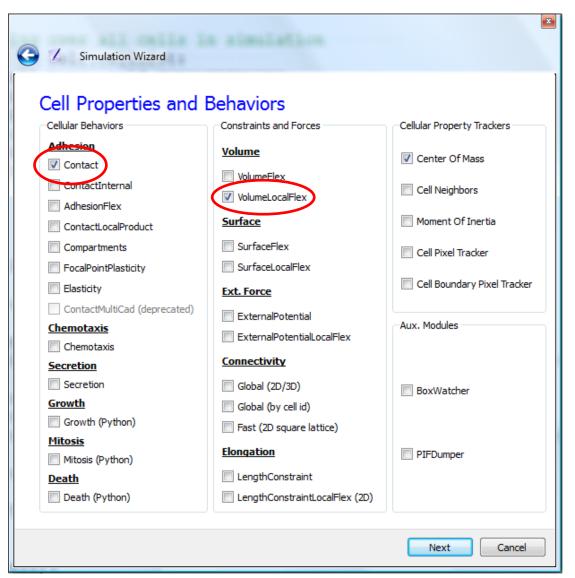
• Make the cell lattice 50x50 and the initial layout a blob:



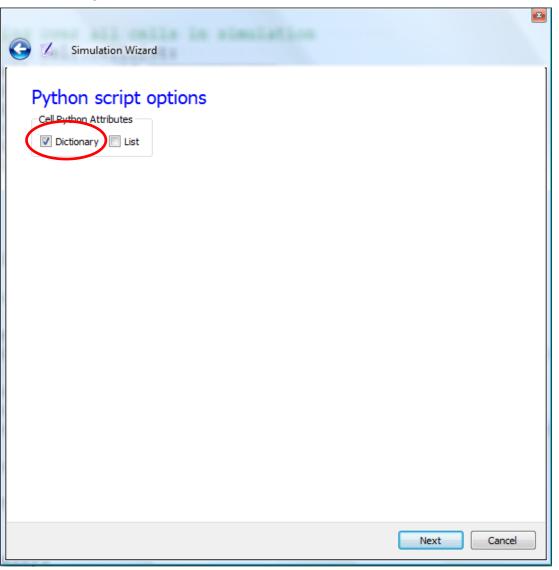
Add cell type "Condensing":



Select Contact and VolumeLocalFlex



Add a dictionary to the cells



- For the simulation to run faster, change the BlobInitializer so that the simulation only has 1 cell:
- If you are using "Python only" option:

```
SteppableElmnt_1=CompuCell3DElmnt.ElementCC3D("Steppable", {"Type":"BlobInitializer"})

RegionElmnt=SteppableElmnt_1.ElementCC3D("Region")

RegionElmnt.ElementCC3D("Center", {"x":"25", "y":"25", "z":"0"})

RegionElmnt.ElementCC3D("Radius", {}, "3")

RegionElmnt.ElementCC3D("Gap", {}, "0")

RegionElmnt.ElementCC3D("Width", {}, "5")

RegionElmnt.ElementCC3D("Types", {}, "Condensing")
```

If you are using XML:

Your Steppable file (CellCycleSteppables.py) will look like that:

```
CellCycleSteppables.py
CC3D Project
                          CellCycle.py
CC3D Simulation
                                  from PySteppables import *

■ CellCycle.cc3d

  Main Python Script
                                  import CompuCell
      CellCycle.py
                                  import sys
  Python
                                 Eclass CellCycleSteppable(SteppableBasePy):
     CellCycleSteppables.py
                                 □ def init (self, simulator, frequency=10):
                                  SteppableBasePy. init (self, simulator, frequency)
                                 ⊟ · · · def · start (self):
                             10
                                  ····· # any code in the start function runs before MCS=0
                             11
                                  -----pass
                                 ⊟ · · · def · step (self, mcs): · · · · · · ·
                                  *** ** #type here the code that will run every frequency MCS
                             13
                                 for cell in self.cellList:
                                  print "cell.id=",cell.id
                                 □ def finish(self):
                                  ** ** * * * * * * Finish · Function · gets · called · after · the · last · MCS
```

Initialize the cell volume constraints:

```
1
2
     from PySteppables import *
     import CompuCell
     import sys
 5
   □class CellCycleSteppable (SteppableBasePy):
   def init (self, simulator, frequency):
     SteppableBasePy.__init__(self,_simulator,_frequency)
10
   def start(self):
     for cell in self.cellList: #setting initial cell volumes
11
          cell.targetVolume=25
12
13
          cell.lambdaVolume=5
14
15
   ☐ def step(self, mcs):
     ** * #type here the code that will run every frequency MCS
16
        for cell in self.cellList:
17
18
    cell.id=", cell.id
19
```

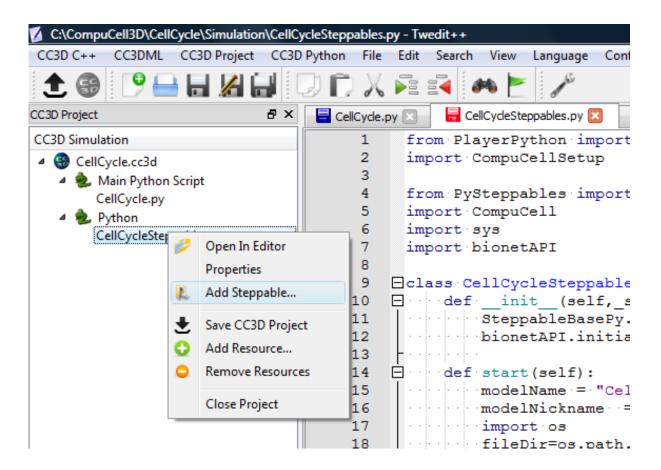
Now fill in the BionetSolver commands:

```
from PySteppables import *
    import CompuCell
    import sys
    import bionetAPI 1
 9
   □class CellCycleSteppable (SteppableBasePy): · · · ·
10
   ☐ def init (self, simulator, frequency):
    SteppableBasePy. init (self, simulator, frequency)
11
    bionetAPI.initializeBionetworkManager(self.simulator)
12
13
    def start(self):
14
15
    □ · · · · · · for · cell · in · self.cellList: #setting · initial · cell · volumes
    cell.targetVolume=25
16
      cell.lambdaVolume=5
17
18
19
        modelNickname = "CC"
20
21
      · · · · · import os
       fileDir=os.path.dirname (os.path.abspath(__file __)) Python utilities
22
       modelPath = fileDir+"\BIOMD000000003.xml"
23
        integrationStep = 0.2 ··
24
25
        bionetAPI.loadSBMLModel(modelName, modelPath, modelNickname, integrationStep)
26
       4 bionetAPI.addSBMLModelToTemplateLibrary(modelName, "Condensing")
27
28
     5 bionetAPI.initializeBionetworks()
29
30
    ☐ · · · def · step (self, mcs):
31
32
          bionetAPI.timestepBionetworks() # iterating the SBML model
33
```

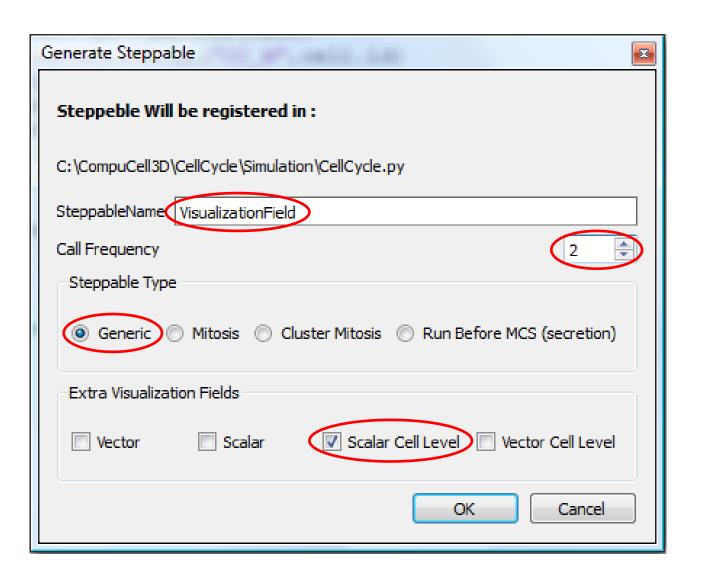
 Right now the simulation should work, the cells are running the SBML model, but we can't see anything.

Let's create a visualization field for the fraction of Cdc2

kinase:



Create a visualization field for the fraction of Cdc2 kinase.



• On the main Python file (*CellCycle.py*) make all frequencies equal to 1:

```
70
      #Add Python steppables here
71
      steppableRegistry=CompuCellSetup.getSteppableRegistry()
72
73
      from CellCycleSteppables import CellCycleSteppable
      steppableInstance=CellCycleSteppable(sim, frequency=1)
74
75
      steppableRegistry.registerSteppable(steppableInstance)
76
77
      from CellCycleSteppables import VisualizationField
      instanceOfVisualizationField=VisualizationField( simulator=sim, frequency=1
78
      steppableRegistry.registerSteppable(instanceOfVisualizationField)
79
80
```

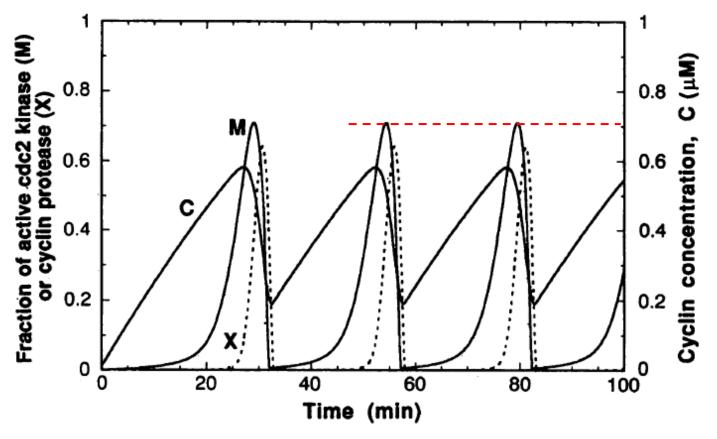
 On the Steppable file (CellCycleSteppables.py) modify/add the following lines:

```
41
42
    □class VisualizationField(SteppableBasePy):

    def init (self, simulator, frequency):
43
      SteppableBasePy. init (self, simulator, frequency)
44
45
      self.scalarCLField=CompuCellSetup.createScalarFieldCellLevelPy("M"
46
47
    ☐ · · · def · step (self, mcs):
48
           clearScalarValueCellLevel(self.scalarCLField)
        for cell in self.cellList:
49
      M=bionetAPI.getBionetworkValue("CC M",cell.id)
50
      fillScalarValueCellLevel(self.scalarCLField,cell,M)
51
52
```

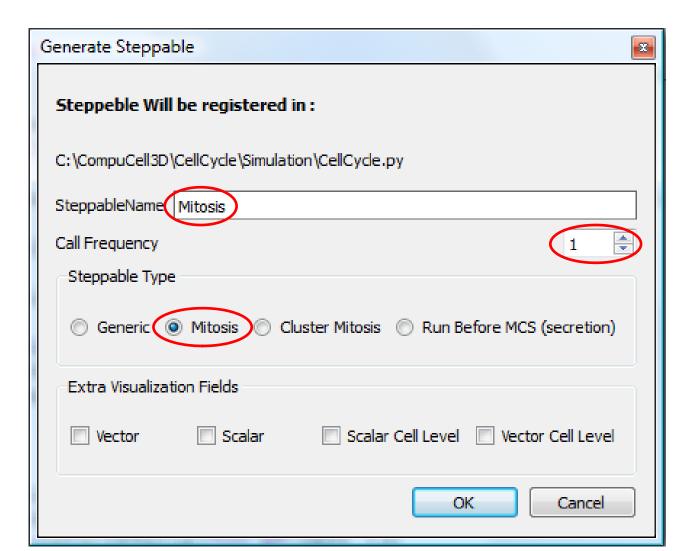
- The first underlined command creates a field called "M"
- The second clears the field every MCS
- The third stores the current value of the M variable
- The last fills the current cell with the stored value

Mitosis occur when fraction of active Cdc2 kinase (M) reaches 0.7.



 To model this we need to track the concentration of M in each cell and check when it passes the 0.7 mark.

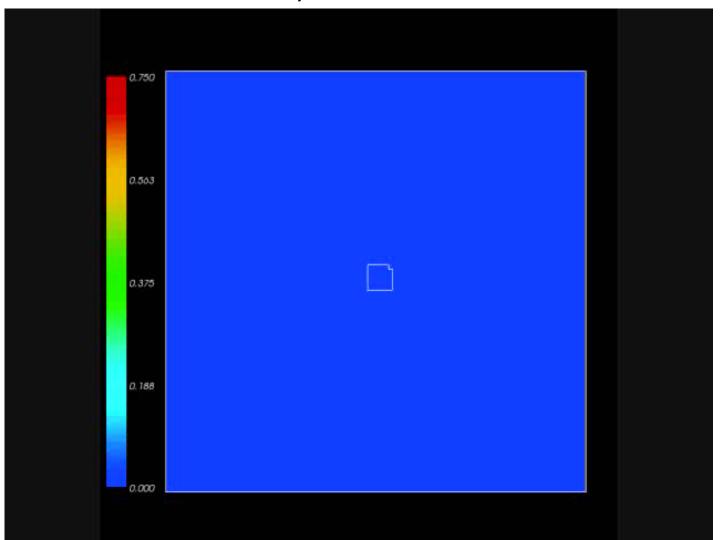
 Add a Steppable to divide cells based on the fraction of Cdc2 kinase:



Go to the Steppable and add the following lines:

```
58
    □class Mitosis (MitosisSteppableBase):
    ☐ · · · def · init (self, simulator, frequency=1):
             MitosisSteppableBase. init (self, simulator, frequency)
60
61
    def start(self):
62
           for cell in self.cellList:
63
                dict attrib=CompuCell.getPyAttrib(cell)
64
65
                dict attrib["M"]=bionetAPI.getBionetworkValue("CC M",cell.id)
66
67
    ☐ · · · def · step (self, mcs):
         cells to divide=[]
68
           for cell in self.cellList:
69
                dict attrib=CompuCell.getPyAttrib(cell)
70
71
                M=bionetAPI.getBionetworkValue("CC M",cell.id)
                 if (M>0.7 and dict attrib["M"]<0.7):
72
                cells to divide.append(cell)
73
                dict attrib["M"]=M
74
          for cell in cells to divide:
75
    self.divideCellRandomOrientation(cell)
76
77
    def updateAttributes(self):
78
79
             parentCell=self.mitosisSteppable.parentCell
             childCell=self.mitosisSteppable.childCell
80
             childCell.targetVolume=parentCell.targetVolume
81
             childCell.lambdaVolume=parentCell.lambdaVolume
82
83
84
             childCell.type=parentCell.type
85
             bionetAPI.copyBionetworkFromParent(parentCell,childCell)
86
             dict attrib Child=CompuCell.getPyAttrib(childCell)
             dict attrib Parent=CompuCell.qetPyAttrib(parentCell)
87
             dict attrib Child["M"]=dict attrib Parent["M"]
88
```

 Open the model in CC3D, set the maximum concentration of the "M" field to 0.75, and run the simulation:



Exercises

• 1

 Change the Volume plugin so that cells slowly grow back to the original target Volume after mitosis

• 2

 Add a second cell type (NonCondensing) with half of the cycle time

- In the last example all cells divide in synchrony.
- The reason for this is the absence of any flow of information from the cell level to the subcellular level.
- A more realistic model, where the cells do not maintain their cell cycle's phase, is the one proposed by Tyson and Novak.

 This model has 5 variables, from which only the first 2 forms the core of the cell cycle oscillations:

$$\frac{\text{d}[\text{CycB}]}{\text{d}t} = k_1 - (k_2' + k_2'') [\text{Cdh1}] [\text{CycB}],$$

$$\frac{\text{d}[\text{Cdh1}]}{\text{d}t} = \frac{(k_3' + k_3'')(1 - [\text{Cdh1}])}{J_3 + 1 - [\text{Cdh1}]} - \frac{k_4 m [\text{CycB}] [\text{Cdh1}]}{J_4 + [\text{Cdh1}]},$$

$$\frac{\text{d}[\text{Cdc20}_T]}{\text{d}t} = k_5' + k_5'' \frac{([\text{CycB}] m/J_5)^n}{1 + ([\text{CycB}] m/J_5)^n} - k_6 [\text{Cdc20}_T],$$

$$\frac{\text{d}[\text{Cdc20}_A]}{\text{d}t} = \frac{k_7 [\text{IEP}] ([\text{Cdc20}_T] - [\text{Cdc20}_A])}{J_7 + [\text{Cdc20}_T] - [\text{Cdc20}_A]} - \frac{k_8 [\text{Mad}] \cdot [\text{Cdc20}_A]}{J_8 + [\text{Cdc20}_A]} - k_6 [\text{Cdc20}_A],$$

$$\frac{\text{d}[\text{IEP}]}{\text{d}t} = k_9 m [\text{CycB}] (1 - [\text{IEP}]) - k_{10} [\text{IEP}].$$

 The crucial difference from the previous model lies in the presence of the parameter "m", which is the normalized total mass of the cell:

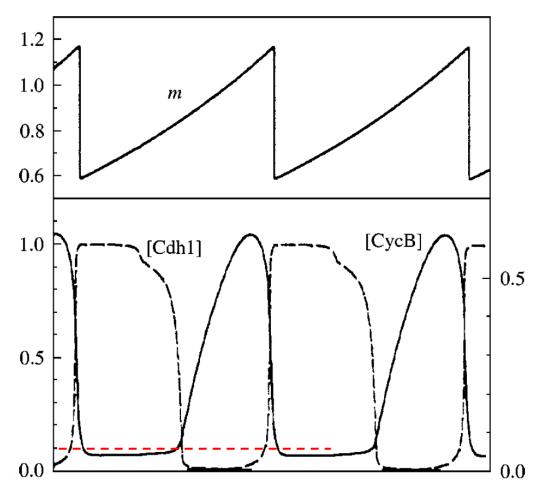
$$\frac{d[\text{CycB}]}{dt} = k_1 - (k'_2 + k''_2 \text{ [Cdh1]}) \text{ [CycB]},$$

$$\frac{d[\text{Cdh1}]}{dt} = \frac{(k'_3 + k''_3 A)(1 - \text{ [Cdh1]})}{J_3 + 1 - \text{ [Cdh1]}} - \frac{k_4 \text{ m} \text{ [CycB] [Cdh1]}}{J_4 + \text{ [Cdh1]}},$$

 This parameter varies between ~0.5 (right after mitosis) and ~1 (at normal size) and corresponds in CC3D to the ratio of volume to the resting volume (initial volume):

$$V_{\sigma}/V_{0}$$

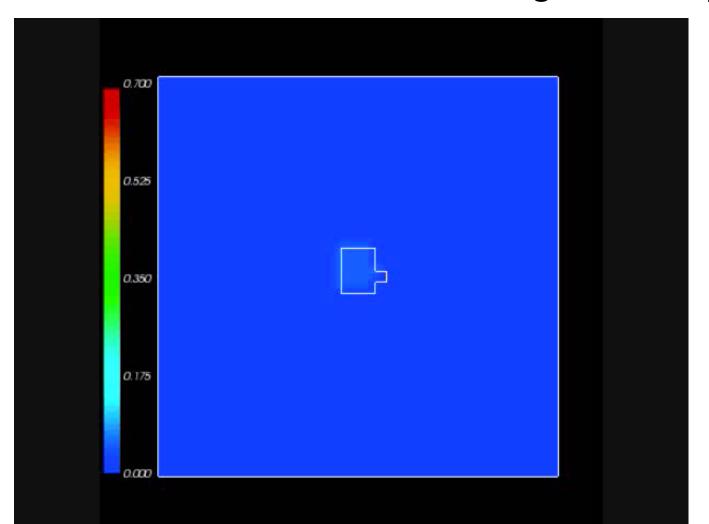
This time mitosis occur when the level of CycB drops below 0.1



Exercises

- 1
 - Download the paper by Tyson and Novak
 - Code the first two ODEs in Jarnac and generate the SBML
- 2
 - Using the code from the second example as a template,
 create a model that uses Tyson's cell cycle

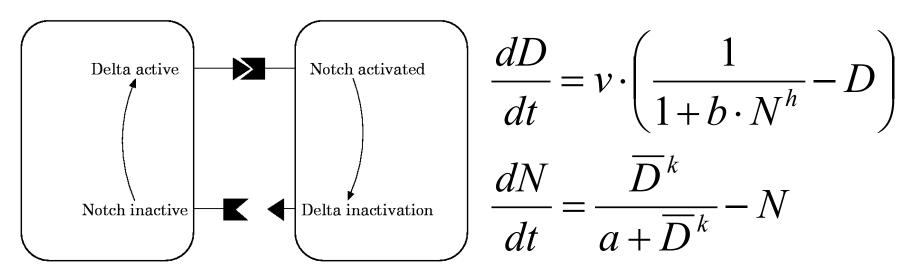
 When we run this model we can see that due to the fluctuations in cell volume the divisions get out of sync:



The third example (Tyson's cell cycle model)
illustrated how changes at the single cell level can
affect the subcellular level (and in turn affect the
cell behavior by initiating mitosis).

This last example will show how conditions
 external to the cell (the neighboring cells' Delta)
 can affect the cell internal state (its Notch levels).

We will use the model published by Collier et al. in 1996:

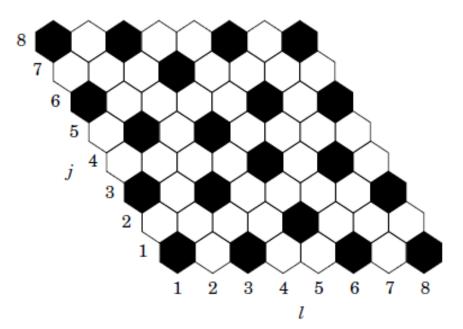


- N: Notch

– D : Delta

− D̄: average Delta from neighbors

- In this model, when a cell receives high levels of Delta from neighbors its Notch level becomes downregulated.
- This leads to the high/low Notch patterning shown by their simulations on an hexagonal lattice:



In CC3D we first loop over all cells' neighbors and store their Delta:

```
def step(self,mcs):
39
         for cell in self.cellList:
40
           D=0.0; nn=0 <
           cellNeighborList=self.getCellNeighbors(cell)
41
           for neighbor in cellNeighborList:
42
43
             if (neighbor.neighborAddress):
44
               D+=bionetAPI.getBionetworkValue("DN D",neighbor.neighborAddress.id)
4.5
           if (nn>0):
46
47
             D=D/nn <
           bionetAPI.setBionetworkValue("DN Davg", D, cell.id) <
48
           cellDict=CompuCell.getPyAttrib(cell)
49
           cellDict["D"]=D
50
           cellDict["N"]=bionetAPI.getBionetworkValue("DN N",cell.id)
51
       bionetAPI.timestepBionetworks()
52
```

- Then we average it and use it as the new D parameter of that cell:-
- File:

 $CompuCell3D \backslash Demos \backslash BoolChapterDemos_Computational Methods In Cell Biology \backslash Delta Notch$

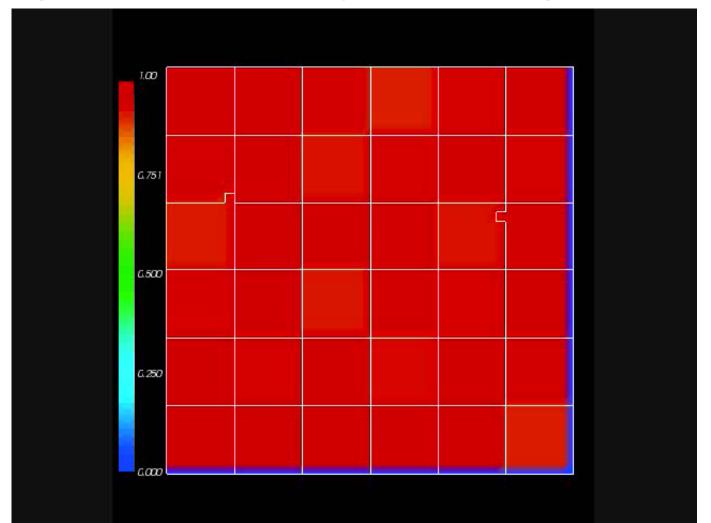
- As an initial condition all cells start with random values of Delta and Notch around 0.9.
- To implement this we use the Python random function as shown below:

```
#Initial conditions
25
26
          import random
27
         for cell in self.cellList:
28
            if (cell):
29
             D = random.uniform(0.9,1.0)
             N = random.uniform(0.9,1.0)
30
             bionetAPI.setBionetworkValue("DN D",D,cell.id)
31
             bionetAPI.setBionetworkValue("DN N", N, cell.id)
32
33
             cellDict=CompuCell.getPyAttrib(cell)
34
              cellDict["D"]=D
              cellDict["N"]=N
35
```

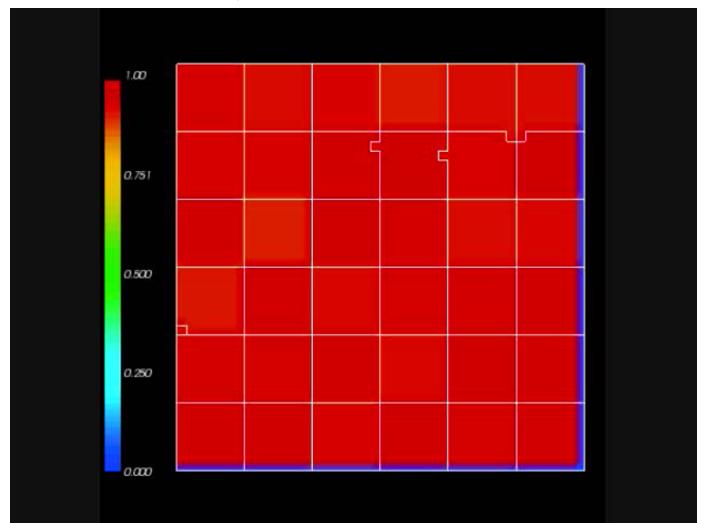
File:

CompuCell3D\Demos\BoolChapterDemos_ComputationalMethodsInCellBiology\DeltaNotch

 When we run this model we can see that first the Notch values go down before the pattern emerges:



• If we increase the level of membrane fluctuations the pattern will be disrupted :



Exercise – 2 SBML models

 Below is a simulation with Tyson's Cell Cycle and Collier's Delta Notch models:

